

Ellipsoid

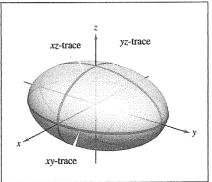
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$$

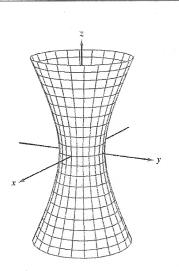
Trace Ellipse

Plane
Parallel to xy-plane

Ellipse Parallel to xz-plane Ellipse Parallel to yz-plane

The surface is a sphere if $a = b = c \neq 0$.





Hyperboloid of One Sheet

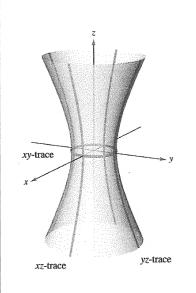
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 1$$

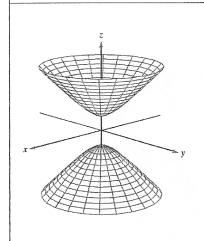
Trace

Plane

Ellipse Parallel to xy-plane Hyperbola Parallel to xz-plane Hyperbola Parallel to yz-plane

The axis of the hyperboloid corresponds to the variable whose coefficient is negative.





Hyperboloid of Two Sheets

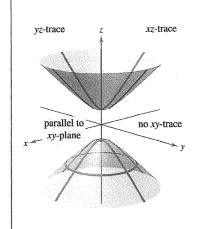
$$\frac{z^2}{c^2} - \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

Trace

Plane

Ellipse Parallel to xy-plane Hyperbola Parallel to xz-plane Hyperbola Parallel to yz-plane

The axis of the hyperboloid corresponds to the variable whose coefficient is positive. There is no trace in the coordinate plane perpendicular to this axis.



x y

Elliptic Cone

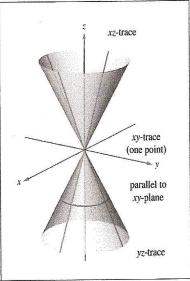
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 0$$

Trace

Plane

Ellipse Parallel to xy-plane Hyperbola Parallel to xz-plane Hyperbola Parallel to yz-plane

The axis of the cone corresponds to the variable whose coefficient is negative. The traces in the coordinate planes parallel to this axis are intersecting lines.



Elliptic Paraboloid

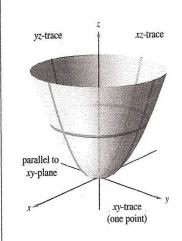
$$z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$$

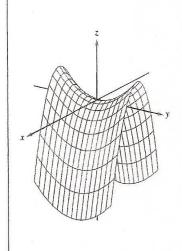
Trace

Plane

Ellipse Parallel to xy-plane
Parabola Parallel to xz-plane
Parabola Parallel to yz-plane

The axis of the paraboloid corresponds to the variable raised to the first power.





Hyperbolic Paraboloid

$$z = \frac{y^2}{b^2} - \frac{x^2}{a^2}$$

Trace

Plane

Hyperbola Parallel to xy-plane
Parabola Parallel to xz-plane
Parabola Parallel to yz-plane

The axis of the paraboloid corresponds to the variable raised to the first power.

